



A Novel Blind Digital Watermarking Based on SVD and Extreme Learning Machine

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ABSTRACT

Modification of media and illegal production is a big problem now a days because of free availability of digital media. Protection and securing the digital data is a challenge. An Integer Wavelet Transformation (IWT) domain based robust watermarking scheme with Singular Value Decomposition (SVD) and Extreme Learning Machine (ELM) have been proposed and tested on different images. In this proposed scheme, a watermark or logo is embedded in the IWT domain as ownership information with SVD and ELM is trained to learn the relationship between the original coefficient and the watermarked one. This trained ELM is used in the extraction process to extract the embedded logo from the image. Experimental results show that the proposed watermarking scheme is robust against various image attacks like Blurring, Noise, Cropping, Rotation, Sharpening etc. Performance analysis of proposed watermarking scheme is measured with Peak Signal to Noise Ratio (PSNR) and Bit Error Rate (BER).

Keywords: IWT, SVD, ELM, PSNR, BER.

INTRODUCTION

With the invention and expansion of internet, data in digital form is distributed and copied easily worldwide. But with the distribution, protection or security of data is equally important. Watermarking is an emerging technique for the security of data. *Watermarking is the process that embeds data called a watermark, tag or label into a multimedia object such that watermark can be detected or extracted later to prove the ownership*¹. Its applications include broadcast monitoring, data authentication, protection of

ownership etc¹. Over the past years, many singular value decomposition (SVD) based watermarking schemes are proposed^{2,3,4}, in which three matrices are modified slightly to embed the watermark. Later, all these SVD based watermarking algorithms are extended to embed the watermark in wavelet domains to provide better robustness⁵. We are proposing a method with the combination of SVD and Extreme Learning Machine (ELM) in Integer Wavelet Domain (IWT). ELM is an algorithm for *single layer feed forward neural network*, where parameters of neural network like weights and bias are randomly selected. Training time of ELM is very

fast since weights and bias are not adjusted by using gradient descent method⁶. Gradient descent method have the problem of slow learning rate, local minima etc. IWT domain reduces the signal loss during the inverse process.

Rest of the paper is organized as follows. We give some background theories about IWT, SVD and ELM in Section 2. Proposed water marking schemes watermark embedding, ELM training and watermark extraction are described in Section 3.

Experimental results are discussed in Section 4 followed by conclusion in Section 5.

**Literature Surcey Of Iwt, Svd And Elm
Integer Wavelet Transform (IWT)**

To increase the robustness, watermarks are to be embedded in wavelet domain instead of spatial domain. The image is divided into low and high resolution bands (*LL,HL,LH,HH*). In discrete wavelet transform, we hide data into floating point coefficients, so during the inverse transformation, any truncation in floating point value leads to the loss of information. IWT transforms a data set into another integer data set⁷. So during forward and inverse transformation, no loss of information is there which leads to have a very close copy of original image⁸. Lifting schemes are used to perform IWT. IWT process is divided into three steps⁹.

1. Split: Partition the data set β_j into low and high frequency samples.
Split $(\beta_j) = \{\text{odd}(\beta_j), \text{even}(\beta_j)\} = \{\gamma_j, \gamma_j\}$
2. Predict: Predict the odd elements γ_j from the even elements λ_j
3. Update: Update the data in the set with the data in the set.

Singular Value Decomposition (SVD)

In linear algebra, SVD is a technique to factorize a rectangular matrix into three decomposition matrices

$$I_{m \times n} = U_{m \times m} D_{m \times n} V_{n \times n}^T \quad \dots(1)$$

$$= [u_1, u_2, \dots, u_m] * \begin{pmatrix} d_1 & 0 & 0 \\ 0 & d_2 & 0 \\ 0 & 0 & d_n \end{pmatrix} * [v_1, v_2, \dots, v_n] \quad \dots(2)$$

By multiply U, D, V^T , we can get the matrix I_{back} .

$$I_{m \times n} = U_{m \times m} * D_{m \times n} * V_{n \times n}^T \quad \dots(3)$$

The diagonal entries d_1, d_2, \dots, d_n in diagonal matrix D are called the singular values. They are related with the image luminance while the U and V the horizontal and vertical details of image determine the “geometry” of the image¹⁰. SVD is a popular method for image watermarking algorithm as singular values are robust against various common image processing operations and geometric transformations like scaling, rotation, translation etc¹¹.

Extreme Learning Machine (ELM)

ELM algorithm is proposed by Huang *et al.*¹² which is based on SLFNs. ELM overcomes the pitfalls of Artificial Neural Network like local minima and slow learning rate. Consider a SLFN with N input layer, M output layer with L hidden neuron. Take N samples where x is vector and o is M output vector. Randomly select two parameters, bias and weights where w is the weight vector of the connection between j^{th} input layer and k^{th} hidden neuron of input layer. The output function T with activation function is given by

$$T_L(x) = \sum_{i=1}^L \beta_i g_i(x) = \sum_{i=1}^L \beta_i G(w_i, b_i, x) = o_i \quad \dots(5)$$

Where w is the weight vector connecting the j^{th} hidden node and the output nodes, b_i is the threshold value of j^{th} hidden nodes. For additive hidden nodes the activation function is defined as

$$G(w_i, b_i, x) = g(w_i \cdot x + b_i) \quad \dots(6)$$

Where w_i denotes the inner product of vector and x in n . For an RBF hidden node the activation function $g(x)$ is given by

$$G(w_i, b_i, x) = g(b_i || x - w_i ||) \quad \dots(7)$$

Where w_i and b_i are the center and the impact factor of the j^{th} RBF node. Equation (4) can be re-written as

$$H\beta = T \quad \dots(8)$$

Where H is the hidden layer output matrix and T is the target vector. are estimated as

$$\beta = H^+T \quad \dots(9)$$

Where H^+ is the Moore-Penrose generalized pseudo inverse¹³.

Essence of ELM

The basic essence of ELM is that:

- 1) No iterative tuning is required in SLFN, , parameters of hidden layer are randomly chosen^{12,14}.
- 2) $\|H\beta - T\|$, the training error and , norm of output weight need to be minimized^{12,14,15}.
- 3) Least square method is used to calculate between the hidden layer and the output layer^{16,6}.

Algorithm

ELM algorithm is as follows: For N training samples $(x_i, t_i) \in R^N \times R^M$, L number of hidden neurons and $g(x)$ as an activation function

- 1) Input weight W_i and bias b_i are randomly generated, where $i=1, \dots, N$
- 2) Calculate H , hidden neuron output matrix.
- 3) Calculate β , output weight using equation $\beta = H^+T$

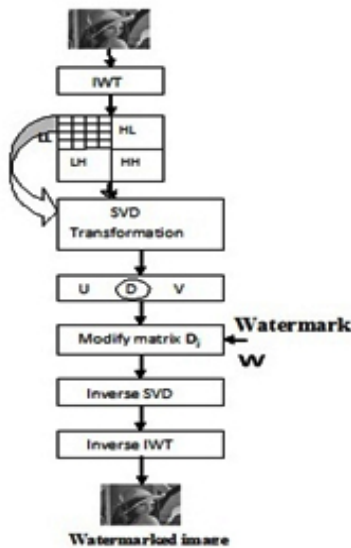


Fig.1: Proposed Watermark embedding process

Proposed Watermarking Scheme

This algorithm consists of three parts: Watermark embedding, ELM Training and Watermark extraction

Watermark Embedding

The block diagram of watermark embedding is shown in Fig(1).

Let us assume there is a host image H , of size and a binary watermark image w with size . As it is a binary image so . In our case, size of image H is and watermark is. The embedding algorithm is as follows:

1. Host image H is transferred through 1-level IWT to decomposed into (LL, LH, HL, HH) sub-bands.
2. Out of these four sub-bands (LL, LH, HL, HH) , LL (Lowest level) has been selected for watermark embedding as it contains maximum energy. Now LL_{ij} sub-band is partitioned into 4×4 non-overlapping coefficient blocks.
3. Apply SVD on each blocks to get three components, U_{ij}, D_{ij} and V_{ij}
4. Take out the four singular values of each LL_{ij}

$$D_{ij} = (d_1, d_2, d_3, d_4)$$

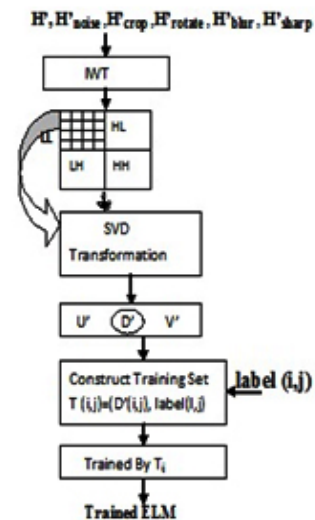


Fig.2. ELM Training Process

- Modify the values of d_2 based on the following mathematical operations where α is embedding strength of watermarking scheme

$$d_2 = \begin{cases} \mu + \alpha \times \delta, & \text{if } w_{ij} = 1 \text{ and } d_2 < \mu \\ d_2, & \text{if } w_{ij} = 1 \text{ and } d_2 > \mu \\ \mu - \alpha \times \delta, & \text{if } w_{ij} = 0 \text{ and } d_2 > \mu \\ d_2, & \text{if } w_{ij} = 0 \text{ and } d_2 < \mu \end{cases}$$

$$\mu = \frac{1}{4} \times \sum_{i=1}^4 d_i$$

$$\delta = \frac{1}{4} \times \sum_{i=1}^4 (d_i - \mu)^2 \quad \dots(10)$$

- Perform inverse SVD to get the modified coefficient block.

$$U_{ij} D'_{ij} V_{ijT} = LL'_{ij} \quad \dots(11)$$
- Perform inverse IWT with LL'_{ij} , HL, LH, HH to get the final watermarked image H' .

ELM Training

The block diagram to train an ELM is shown in fig (2).

Training set is derived from the original watermarked image H' and the corrupted watermarked images by Gaussian noise H'_{noise} , cropping H'_{crop} , rotation H'_{rotate} , blurring H'_{blur} , sharpening H'_{sharp} respectively. Training of ELM is as follows:

- Apply IWT on H' , H'_{noise} , H'_{crop} , H'_{rotate} , H'_{blur} , H'_{sharp} and get their respective LL sub-bands denoted as LL' , LL'_{noise} , LL'_{crop} , LL'_{rotate} , LL'_{blur} , LL'_{sharp}
- Each LL sub-band (LL' , LL'_{noise} , LL'_{crop} , LL'_{rotate} , LL'_{blur} , LL'_{sharp}) is divided into non-overlapping coefficient blocks.
- Apply SVD on each blocks to get the singular values of each image $D_{ij} = (d_1, d_2, d_3, d_4)$
- Take each sample label according to the following equation

$$label_{ij} = \begin{cases} 1 & \text{if } W_{ij} = 1 \\ 2 & \text{if } W_{ij} = 0 \end{cases} \quad \dots(12)$$

- Construct the training set with feature vector D_{ij} and label $label_{ij}$

$$T^k_{ij} = (D_{ij}, label_{ij}), k=1, \dots, 6 \text{ and } i \leq N \text{ and } j \leq N$$
- Train the ELM with the training set T^k_{ij} .

Watermark Extraction

The block diagram to extract the watermark is shown in fig (3)

- The process is as follows:
- Apply IWT on watermarked image H' to get LL' sub-band.
 - Partition LL' sub-band into 4×4 non-overlapping coefficient blocks.
 - Apply SVD on LL'_{ij} to get the feature vector $D'_{ij} = (d'_1, d'_2, d'_3, d'_4)$
 - By using well trained ELM, get the predicted label $label'_{ij}$ corresponding to each D'_{ij} .
 - Watermark can be extracted by using the predicted label as

$$W'_{ij} = \begin{cases} 1 & \text{if } label'_{ij} = 1 \\ 0 & \text{if } label'_{ij} = 2 \end{cases} \quad \dots(13)$$

Experimental Results For Robustness Of The Proposed Watermarking Scheme

In this paper, an experiment is performed on host images like Lena, Baboon, Pepper, Elaine and Jet of size 512×512 and a watermark logo of size 32×32 is used. The value of ∞ is taken as 0.3 Performance of watermarking algorithm is done on the basis of two parameters imperceptibility and robustness. PSNR is used to measure the quality of watermarked image with the original host image. Higher the value of PSNR, better is the quality of watermarked images. PSNR between the original image and watermarked image H and H' is¹⁷.

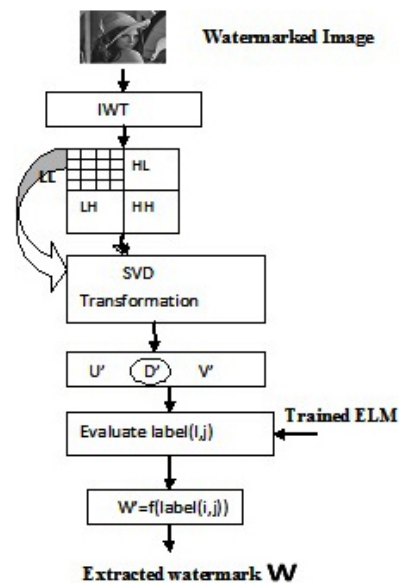


Fig. 3: Proposed Watermark Extraction process

$$PSNR = 10 \log \log_{10} \frac{255 \times 255}{\sum_{i=0}^{m-1} \sum_{j=0}^{n-1} (x_{ij} - x'_{ij})^2} / (m \times n) \dots(14)$$

and BER is evaluated as

$$BER = \sum_{t=1}^{p \times q} (w_t \oplus w'_t) / p \times q \dots(15)$$

where w_t is original watermark and w'_t is the extracted watermark. $p \times q$ is the size of

watermark and \oplus is an exclusive-OR operator. Lower the value of BER implies greater similarity between the extracted watermark and the original one.

The value of α is tested in the interval $\alpha \in [0, 0.3]$. It is found that the value of PSNR is decreasing with the value of α as shown in Fig(4).

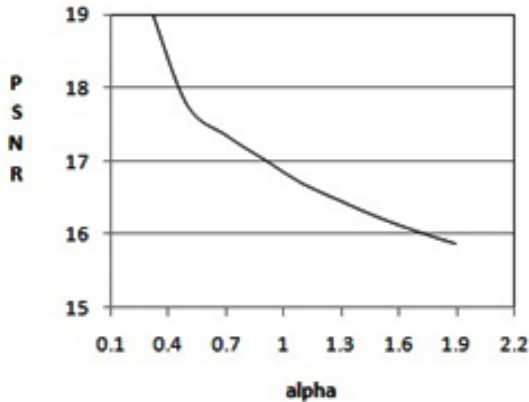


Fig.4: Relation between PSNR and α .

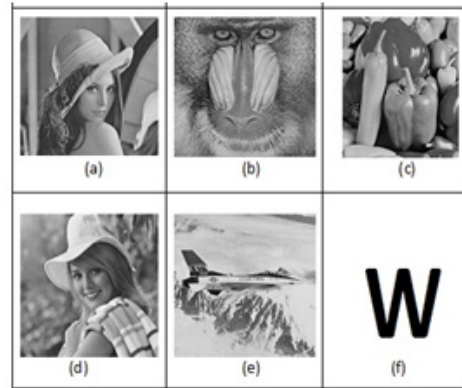


Fig.5: (a) Lena (b) Baboon (c) Peppers (d) Elaine (e) Jetplane images used for watermarking and (f) the Watermark logo

Table 1: Attacked Lena images, corresponding value of BER, PSNR and extracted binary watermark (ownership) from attacked watermarked Lena image by using the proposed watermarking scheme

Attacks	Image	BER	PSNR	Ownership
Blurring		0.0205	23.06	
Cropping		0.1074	21.70	
Noise		0.0218	18.7039	
Rotation		0.1441	17.4914	
Sharpening		0.0469	18.0145	

Table 2: Attacked Baboon images, corresponding value of BER, PSNR and extracted binary watermark (ownership) from attacked watermarked Baboon image by using the proposed watermarking scheme

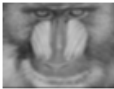

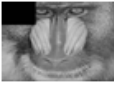







Attacks	Image	BER	PSNR	Ownership
Blurring		0.0332	19.3670	
Cropping		0.0850	21.3491	
Noise		0.0928	18.2904	
Rotation		0.1001	15.3847	
Sharpening		0.0329	14.2370	

Table 3: Attacked Peppers images, corresponding value of BER, PSNR and extracted binary watermark (ownership) from attacked watermarked Peppers image by using the proposed watermarking scheme











Attacks	Image	BER	PSNR	Ownership
Blurring		0.0405	27.6210	
Cropping		0.0947	27.2009	
Noise		0.0752	23.5349	
Rotation		0.1121	21.5885	
Sharpening		0.0596	23.6203	

Table 4: Attacked Elaine images, corresponding value of BER, PSNR and extracted binary watermark (ownership) from attacked watermarked Elaine image by using the proposed watermarking scheme





















Attacks	Image	BER	PSNR	Ownership
Blurring		0.0869	23.8083	
Cropping		0.0215	17.9941	
Noise		0.0113	16.9005	
Rotation		0.1022	16.1664	
Sharpening		0.0669	15.1334	

Table 5: Attacked Jetplane images, corresponding value of BER, PSNR and extracted binary watermark (ownership) from attacked watermarked Jetplane image by using the proposed watermarking scheme

Attacks	Image	BER	PSNR	Ownership
Blurring		0.0415	25.9971	
Cropping		0.1055	25.6287	
Noise		0.0635	23.0474	
Rotation		0.1078	20.1516	
Sharpening		0.0613	23.2219	

CONCLUSIONS

In this paper, we proposed a novel combination of IWT, SVD and ELM for authentication of ownership. In the proposed scheme, host image is transformed in IWT domain and then LL sub-band is used to take the singular values, where required numerical operations are done to embed

the watermark. Watermark extraction is a two-step process, firstly training of ELM and secondly the actual watermark extraction for proof of ownership. As shown in experimental results, our proposed method is robust against various attacks and the extracted watermark, to prove the ownership is very much similar to the original watermark, i.e. less BER value.

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